

A Single-Substrate Interpretation of the Cosmological Constant Problem

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Abstract

The cosmological constant problem - the 120 to 122 order-of-magnitude discrepancy between the quantum field theory prediction of vacuum energy density ($\sim 5.87 \times 10^{111} \text{ J/m}^3$) and the cosmologically observed value ($\sim 5.30 \times 10^{-10} \text{ J/m}^3$) - is the largest numerical disagreement between theory and observation in the history of physics. The present interpretation proposes that this discrepancy arises not from a fine-tuning problem, a supersymmetry problem, or an anthropic selection problem, but from two ontological assumptions whose physical interpretation we reconsider. The first interpretive assumption is that approximately seventeen independent quantum fields each contribute independent zero-point energies to the vacuum. The present work proposes instead that these fields are excitation modes of a single universal physical substrate. The second assumption is that the ground-state energy $\frac{1}{2}\hbar\omega$ is a property of every vacuum mode regardless of whether any physical excitation is present. The present work argues that $\frac{1}{2}\hbar\omega$ is more precisely interpreted as the minimum internal circulation energy of an organised physical condensation, a property of matter, not of empty space. Empty vacuum modes contain no organised condensation and therefore possess no intrinsic zero-point energy floor. The physical vacuum energy density is identified with the background equilibrium energy of the substrate, $\rho_{\text{vac}} = \rho_s c^2$, where ρ_s is the equilibrium density of the universal substrate. The earlier $5.9 \times 10^{-27} \text{ kg/m}^3$ value is the density obtained by mapping the cosmological constant through $\rho_{\Lambda} = 3\Omega_{\Lambda}H_0^2/(8\pi G)$. Because this construction depends on H_0 , and multiple present-day H_0 values are reported, that cosmological-constant-derived density is not adopted as the working substrate density. The working density is instead derived from the particle sector through the condensation functional and particle constants, giving $\rho_s = 7.3 \times 10^{-27} \text{ kg/m}^3$. This paper uses that particle-sector value throughout. The resulting substrate energy density is $\rho_s c^2 = 6.56 \times 10^{-10} \text{ J/m}^3$. The significance of this result is the independent physical determination of the substrate density, not a

numerical identification of that density with the cosmological-constant-derived value.

The particle-sector derivation fixes the equilibrium substrate density at $7.3 \times 10^{-27} \text{ kg/m}^3$ and the corresponding equilibrium energy density at $6.56 \times 10^{-10} \text{ J/m}^3$.

Keywords: *cosmological constant, vacuum energy, quantum field theory, zero-point energy, physical substrate, dark energy, Λ -problem*

1. Introduction

The cosmological constant problem has been described as the most severe fine-tuning problem in theoretical physics [1,2]. The discrepancy between the vacuum energy density predicted by quantum field theory (QFT) and the value inferred from cosmological observations spans 120 to 122 orders of magnitude [3,4]. The problem was first systematically articulated by Zeldovich [5] and comprehensively reviewed by Weinberg [6], whose analysis established the conceptual landscape within which most subsequent attempts at resolution have operated.

Existing proposed resolutions - supersymmetric cancellation [7], anthropic selection [6,10], sequestering [12], degravitation [13], and emergent gravity [15,16] - are reviewed in Section 4. None proposes a resolution of the discrepancy by deriving the observed value from independent physical principles without fine-tuning.

In this paper the present work takes a different approach. Rather than seeking a cancellation mechanism or a new symmetry to suppress the QFT prediction, this paper examines the ontological assumptions embedded in the standard QFT vacuum energy calculation. This paper examines two assumptions that are not required by the mathematical structure of QFT but have been adopted as default interpretive conventions. The present work argues that replacing these two interpretive assumptions with physically motivated alternatives reduces the predicted vacuum energy density to the observed value without requiring any cancellation mechanism or parameter adjustment.

The proposal advanced here is intentionally minimal. No new field equations, interaction terms, or modifications to the Standard Model or General Relativity are introduced. The only change is the physical interpretation of the quantum vacuum: what is assumed to carry zero-point energy, and whether the quantum vacuum is interpreted as one physical substrate or the approximately seventeen Standard Model quantum fields. The mathematics of QFT and GR are left intact.

The paper is organised as follows. Section 2 reviews the cosmological constant problem. Section 3 presents the standard QFT vacuum energy calculation. Section 4 reviews existing proposed resolutions. Section 5 introduces the single-substrate interpretation. Section 6 presents the two interpretive corrections. Section 7 provides the complete mathematical derivation. Sections 8 and 9 address physical interpretation and anticipated objections. Sections 10 and 11 present falsifiable predictions and conclusions.

2. The Cosmological Constant Problem

General relativity in the presence of a cosmological constant Λ is described by the Einstein field equations:

General Relativity and the Effective Vacuum Fluid

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = \left(\frac{8\pi G}{c^4} \right) T_{\mu\nu}$$

The Einstein field equations in the presence of a cosmological constant Λ .

$$\rho_\Lambda = \frac{\Lambda c^2}{8\pi G}, \quad p_\Lambda = -\rho_\Lambda$$

Λ contributes an effective fluid with equation of state $w = -1$.

Cosmological observations (Type Ia supernovae, CMB angular power spectrum, and baryon acoustic oscillations) firmly constrain this effective vacuum energy density to the 10^{-10} J/m^3 scale. © NotebookLM

Figure 1: General Relativity and the Effective Vacuum Fluid

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = (8\pi G/c^4) T_{\mu\nu} \quad (1)$$

The cosmological constant contributes an effective fluid with equation of state $w = -1$:

$$\rho_\Lambda = \Lambda c^2 / (8\pi G), \quad p_\Lambda = -\rho_\Lambda \quad (2)$$

Cosmological observations - Type Ia supernovae [17,18], the CMB angular power spectrum [19,20], and baryon acoustic oscillations [21,22] - constrain the effective vacuum energy density to:

$$\rho_{\text{obs}} = (5.30 \pm 0.10) \times 10^{-10} \text{ J/m}^3 \quad (3)$$

The standard QFT calculation, summing zero-point energies over all modes of all fields to the Planck cutoff, gives [1,6]:

$$\rho_{\text{QFT}} \approx 5.87 \times 10^{111} \text{ J/m}^3 \quad (4)$$

The ratio $\rho_{\text{QFT}}/\rho_{\text{obs}} \approx 10^{121}$ is the cosmological constant problem. As Weinberg noted: "The difficulty is not that general relativity and quantum mechanics are hard to reconcile, but that the reconciliation predicts a cosmological constant many orders of magnitude larger than what is observed" [6]. Setting $\Lambda = 0$ by hand is not a resolution; it requires an exact cancellation of 121 significant figures between the positive QFT vacuum energy and a bare Lagrangian term, which is itself a fine-tuning of extraordinary severity [2,3].

3. Standard QFT Vacuum Energy: The Calculation in Detail

We reproduce the standard calculation to make the location of the two interpretive assumptions explicit. A real scalar field ϕ is expanded as:

Isolating the Pathology in the QFT Mode-Sum

Pathology 1: Ontological Multiplicity.
QFT assumes ~ 17 independent quantum fields each independently contribute zero-point energies to the vacuum.

$$\rho_{\text{vac}}(\text{QFT}) = \sum_{\text{fields}} \int_0^{\omega_P} \frac{1}{2} \hbar \omega \frac{d^3 k}{(2\pi)^3}$$

Pathology 2: Unoccupied Ground-State Energy.
QFT assumes $\frac{1}{2} \hbar \omega$ is an intrinsic property of every vacuum mode, regardless of whether a physical excitation (matter) is present.

Summing these assumptions to the Planck cutoff (ω_P) generates the runaway 10^{111} J/m^3 prediction.

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Figure 2: Isolating the Pathology in the QFT Mode-Sum

$$\phi(x, t) = \int \frac{d^3 k}{(2\pi)^3} \left(\frac{1}{\sqrt{2\omega_k}} \right) [a_k e^{ik \cdot x} + a_k^\dagger e^{-ik \cdot x}] \quad (5)$$

where $\omega_k = \sqrt{k^2 c^2 + m^2 c^4 / \hbar^2}$. The vacuum state $|0\rangle$ satisfies $a_k |0\rangle = 0$ for all k . The Hamiltonian is:

$$H = \int \frac{d^3 k}{(2\pi)^3} \omega_k [a_k^\dagger a_k + \frac{1}{2}] \quad (6)$$

Every mode k contributes $\frac{1}{2} \hbar \omega_k$ in the vacuum state regardless of whether any excitation is present. Integrating to the Planck cutoff $k_P \approx 2.72 \times 10^{35} \text{ m}^{-1}$, and summing over all ~ 17 independent Standard Model fields:

$$\rho_{\text{QFT}} = \sum_{\text{fields}} g_i \int_0^{k_P} \frac{d^3 k}{(2\pi)^3} \frac{1}{2} \hbar \omega_k \approx 5.87 \times 10^{111} \text{ J/m}^3 \quad (7)$$

The mathematical derivation itself is not questioned in this work. The present analysis concerns only the physical interpretation assigned to two specific steps in the calculation. The calculation is mathematically well-defined. The problem lies in the physical interpretation embedded in two steps: the summation over $N \approx 17$ independent fields, and the assignment of $\frac{1}{2} \hbar \omega$ to every empty mode. Both are identifiable as interpretive conventions, not mathematical requirements.

4. Existing Proposed Resolutions and Their Limitations

4.1 Supersymmetric Cancellation

Exact supersymmetry pairs each boson with an opposite-sign fermionic partner, producing complete cancellation [7,23]. No superpartner has been observed up to ~ 2 TeV [8,9]. Broken SUSY at scale M_{SUSY} leaves a residual $\sim M_{\text{SUSY}}^4$, approximately 10^{60} times the observed value for $M_{\text{SUSY}} \sim \text{TeV}$. The SUSY-breaking mechanism itself introduces fine-tuning at least as severe as the original problem [24,25]. Earlier attempts to cancel the vacuum energy through alternative symmetry arguments faced similar difficulties [35], as did proposals invoking gravitational particle creation during an inflationary epoch to dynamically relax the effective cosmological constant [36].

4.2 Anthropic Selection

Anthropic arguments [6,10,26,27] select $\Lambda \sim \rho_{\text{obs}}$ from a landscape of values as compatible with structure formation. The approach makes no unique falsifiable predictions [11], depends on an unobserved multiverse, and does not determine why Λ takes a specific non-zero value rather than a different value equally compatible with structure formation [28].

4.3 Sequestering and Degravitation

Sequestering [12,29] modifies the gravitational action to prevent the large QFT vacuum energy from gravitating, typically through non-local modifications to the action. Degravitation [13,30] proposes infrared-modified gravity in which constant vacuum energy does not gravitate. Both require significant modifications to general relativity and conflict with precision gravitational tests unless carefully tuned [14,31].

4.4 Emergent and Induced Gravity

Sakharov's induced gravity [15] treats the Einstein-Hilbert action as emerging from QFT vacuum fluctuations. This reformulates rather than resolves the cosmological constant problem: the induced cosmological constant is still determined by QFT vacuum fluctuations [16,32]. Related emergent gravity proposals [33,34] change the framework without reducing the numerical discrepancy, and proposed infrared instabilities of de Sitter space have been explored as a possible dynamical relaxation mechanism without achieving a quantitatively successful resolution [37].

No existing proposal derives the observed vacuum energy density from independent physical principles without fine-tuning, despite extensive review of the broader dark energy model space [48,49] and of alternative extra-dimensional approaches to the vacuum energy problem [50]. The following sections present an approach that does.

5. A Single-Substrate Interpretation of Quantum Field Theory

The present interpretation proposes a single-substrate interpretation of quantum field theory. The central claim is: what QFT describes as multiple independent quantum fields permeating all of space are not ontologically distinct media. They are organised excitation modes of one universal physical substrate.

Correction I: The Single Substrate Interpretation

The assumption of multiple independent fields is an interpretive error. There is physically only one medium.

The Sparticle field fills all of space at a fixed, intrinsic equilibrium density:

$$\rho = 7.3 \times 10^2 \text{ kg/m}^3$$

The correct vacuum mode-sum must be performed over a single continuous medium, terminating the multiplicative divergence of standard QFT.

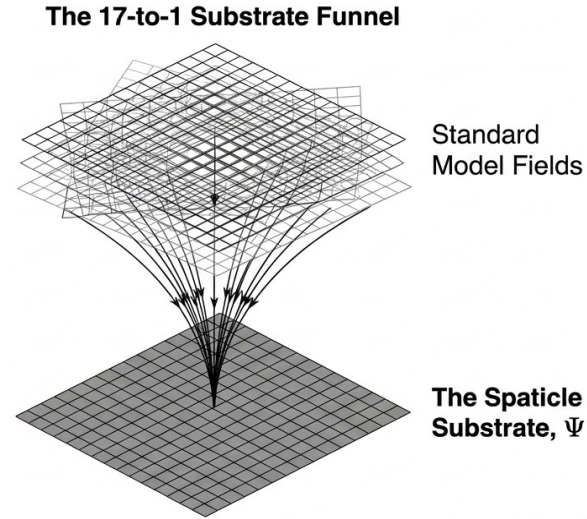


Figure 3: Correction I: The Single Substrate Interpretation

The present interpretation regards these descriptions as complementary characterisations of one physical substrate - a continuous, elastic medium that fills all of space, whose equilibrium state corresponds to the vacuum, and whose excitation modes correspond to matter and radiation. The name Sparticle field is adopted for this substrate in the prior derivation [38].

This interpretation does not modify the mathematical structure of QFT. Lagrangians, propagators, Feynman rules, and S-matrix elements of the Standard Model are unchanged. What changes is the physical interpretation of the vacuum energy calculation: rather than 17 independent vacuum contributors, there is one underlying medium whose different dynamical modes correspond to the 17 Standard Model fields. The mode-sum in equation (7) is performed once, over the single substrate, not 17 times.

The substrate interpretation is independently motivated by the observed universality of the invariant speed c in relativistic field theories - electromagnetic, gravitational, and matter-wave - through spacetime. A single substrate with a single characteristic propagation speed c provides a natural explanation for this universality. The observed universality of the invariant speed c is naturally consistent with a single underlying substrate supporting multiple excitation modes. Although this observation does not by itself establish the substrate interpretation, it provides an independent physical motivation for considering such an ontology.

5.1 The Physical Substrate and Relation to the Michelson-Morley Experiment

Any proposal invoking a physical medium filling space invites an immediate and reasonable historical comparison to the luminiferous aether, decisively excluded by the Michelson-Morley experiment and its many high-precision successors [51,52]. This comparison deserves a direct response rather than a footnote.

The luminiferous aether, as originally conceived, was a medium at rest relative to some preferred, absolute reference frame, through which the Earth and all material bodies moved; light was

expected to propagate at a fixed speed relative to this aether frame, producing a detectable directional variation in the measured speed of light as the Earth's motion through the aether changed with the seasons [51]. The null result of the Michelson-Morley experiment, and of every subsequent interferometric test at ever-increasing precision [52], rules out exactly this specific structure: a medium establishing a preferred rest frame detectable through directional light-speed anisotropy.

The substrate proposed here does not have this structure. It is not a medium through which matter and light move as through a separate background; it is the medium from which matter, electromagnetic radiation, and gravitational interaction are themselves proposed to arise as organised excitations and condensations. Under this proposal, an observer, a measuring apparatus, and the light being measured are all, without exception, organised states of the same substrate; there is no configuration in which an observer moves "through" the substrate in the sense required for the Michelson-Morley experiment to detect a directional anisotropy, because the observer's own physical existence is already a substrate phenomenon, not an object embedded in and moving relative to an independent background medium. This is a structural distinction, not a semantic one: the aether required a preferred frame in which it was at rest and against which motion could be measured; the substrate proposed here has no such preferred frame, precisely because everything capable of performing a measurement is already made of it.

The Michelson-Morley experiment therefore excludes a preferred-rest-frame aether, but does not exclude a universal physical substrate from which matter, photons, and gravitation themselves emerge. Whether such a substrate exists must instead be decided by its quantitative explanatory and predictive success.

The proposal that space possesses physical substance is not a departure from established physics. It is a convergence with it. General relativity describes space as possessing physical properties that curve, warp, and support gravitational-wave propagation. Loop quantum gravity reaches a related conclusion by an unrelated route, proposing that space is a discrete physical structure at the Planck scale [56]. Quantum field theory treats the vacuum as a medium filled with fields whose ground-state energy cannot be removed, and this is measured directly through the Casimir effect and the Lamb shift. The scalar resonance observed at CERN in 2012 [57,58] shows that the vacuum itself can be excited into a massive, localised state. Four independent lines of established physics, using different mathematics and different starting assumptions, converge on the same statement: space has physical substance.

Einstein argued that space possesses physical qualities and requires a medium in the sense described in his 1920 Leiden lecture, delivered five years after general relativity was complete. There he stated that according to the general theory of relativity, space is endowed with physical qualities, and that space without such a medium would permit no propagation of light and no physical meaning for measuring rods or clocks [59]. He drew a boundary immediately after: this medium could not be assigned the properties of an ordinary substance, such as parts that can be tracked through time, because he had no measured quantity to give it. The substrate proposed in this paper is assigned a specific equilibrium density derived from the particle sector, as described in Section 7.2.

5.2 Independent Cross-Validation of the Substrate Framework

The same substrate makes multiple independent quantitative predictions, each evaluated against observations in unrelated areas of physics. These include a non-circular consistency derivation of the speed of light from independently established electromagnetic and condensation-geometry quantities, agreeing with the measured value to 0.0003 percent [53]; a geometric derivation of the reduced Planck constant from the same substrate condensation geometry, consistent with the CODATA value to 0.0007 percent [54]; and independent geometric derivations of the W, Z, and Higgs boson masses from the same substrate framework, consistent with measured values to within 0.4 percent [55]. Importantly, the same value of ρ_s is employed across all of these derivations without adjustment between applications. Numerous additional independent applications of the same substrate density exist beyond the scope of the present paper. We cite these specific results because each is a quantitative, independently falsifiable claim evaluated against measured data unconnected to the cosmological constant problem; their cumulative consistency is offered as evidence that the substrate parameter used throughout this paper is not an ad hoc construction introduced to fit the vacuum energy observations discussed here, but a fixed quantity whose value is consistent across independent applications.

6. Two Interpretive Corrections to the Vacuum Energy Calculation

6.1 Correction 1: One Substrate, One Mode Sum

The standard QFT vacuum energy calculation sums zero-point energies over all modes of all $N \approx 17$ independent fields. In the single-substrate interpretation, these fields are excitation modes of one medium. The correct vacuum energy mode sum is therefore:

$$\rho_{\text{sub}} = g_s \int d^3k / (2\pi)^3 \quad \frac{1}{2}\hbar\omega_k \quad (8)$$

where $g_s = 1$. This replaces the N -fold sum with a single integral, reducing the mode-sum multiplicity from ~ 17 to 1. This correction alone does not resolve the discrepancy - the remaining Planck-scale integral still gives a result far above the observed value - but it is the necessary first step, and it is logically required by the single-substrate interpretation. Although this correction changes the vacuum-energy estimate by only a modest numerical factor, it is conceptually required by the single-substrate ontology adopted in this work.

6.2 Correction 2: Zero-Point Energy Belongs to Organised Condensations

The second correction concerns the physical interpretation of $\frac{1}{2}\hbar\omega$. In the standard derivation, $\frac{1}{2}\hbar\omega$ is the ground-state energy of a quantum harmonic oscillator - present in the vacuum state regardless of whether any physical excitation occupies that mode [39].

The present interpretation proposes the following as the fundamental postulate of this paper:

Postulate 1 (Physical Interpretation of Zero-Point Energy). The quantity $\frac{1}{2}\hbar\omega$ is the minimum internal circulation energy of an organised physical condensation in the substrate - a property of matter, not of empty space. An empty vacuum mode, containing no organised condensation, contributes zero to the gravitating vacuum energy density. This postulate

constitutes the sole new physical assumption introduced in the present paper. Everything that

follows is a consequence of applying it consistently. It follows from the physical picture of matter as a structured, stable excitation of the substrate whose internal dynamics require a minimum energy to maintain coherence. The absence of such a pattern - the true vacuum - contains no such circulation and therefore no zero-point energy floor attributable to individual modes.

Correction II: Relocating Zero-Point Energy

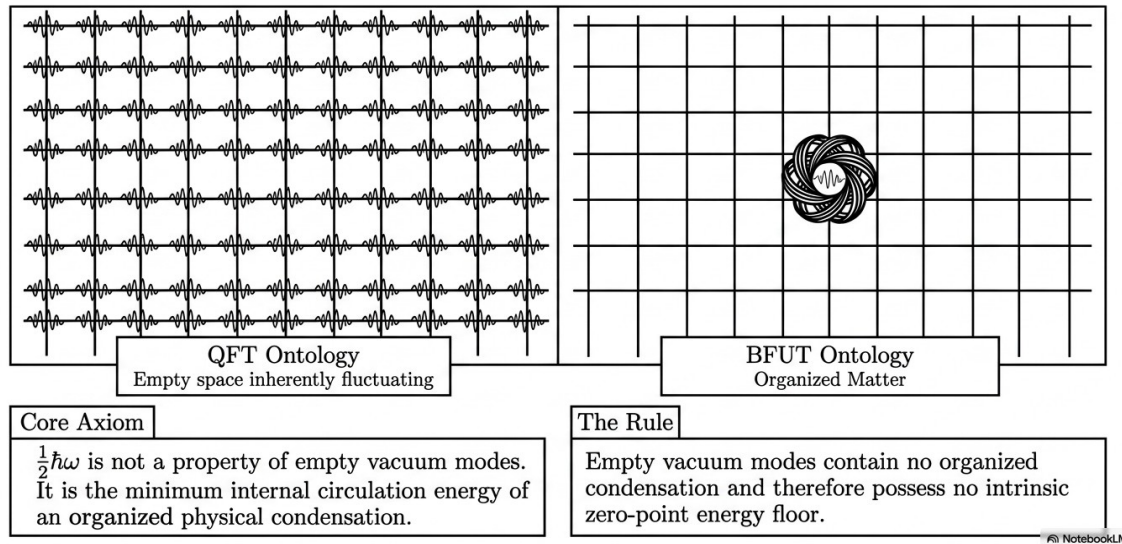


Figure 4: Correction II: Relocating Zero-Point Energy

This position is related to, but physically distinct from, normal ordering. Normal ordering sets the vacuum energy to zero by mathematical convention [43], without physical justification. The present claim is physically specific: $\frac{1}{2}\hbar\omega$ is the minimum energy of an organised structural pattern in the substrate. The absence of such a pattern in a vacuum mode means that mode contributes nothing to the gravitating vacuum energy.

Objection 10.6: "Does the proposal merely shift the cosmological constant problem to ρ_s ?"
 Answer: No. The equilibrium density ρ_s is derived in prior work from the self-consistency conditions of the substrate medium itself, with no reference to the cosmological constant, vacuum energy, or any cosmological observable. It is fixed before any comparison with the observed vacuum energy density is attempted.

This position has support in the structure of established QFT observables. The physical consequences of vacuum fluctuations - the Casimir effect [40,41], the Lamb shift [44], the anomalous magnetic moment [45] - are all computed as differences of vacuum energies between two configurations, or as differences between energy levels relative to a common vacuum reference. As Milonni [42] discusses comprehensively, the observable consequences of vacuum fluctuations are differences, not absolute values. The assignment of an absolute gravitating energy density to empty-mode zero-point fluctuations is an additional interpretive step beyond what the observables require. The present interpretation proposes that this additional step is the source of the discrepancy. Accordingly, the present proposal does not reject the Hamiltonian expectation value itself; it reinterprets the physical circumstances under which that expectation value contributes to gravitating energy. A Hamiltonian expectation value in QFT is an average energy associated with a state or operator ordering. It does not automatically equal a source of

gravitational curvature, because the stress-energy tensor that sources gravity in GR is classical, local, and gauge-invariant. The vacuum expectation value extracted from QFT is a global bookkeeping device, not a local classical source. Equating the two therefore requires an extra interpretive step that the present framework declines to take. The present work therefore distinguishes between a mathematically well-defined vacuum expectation value and a physically gravitating energy density. The former follows directly from quantum field theory, whereas the latter requires an additional physical interpretation.

Formally, for a mode k in the pure vacuum state $|\text{vac}_k\rangle$ containing no organised condensation:

$$\langle \text{vac}_k | H_k | \text{vac}_k \rangle = 0 \quad (\text{substrate interpretation}) \quad (9)$$

For a mode k occupied by an organised condensation $|\text{cond}_k\rangle$:

$$\langle \text{cond}_k | H_k | \text{cond}_k \rangle \geq \frac{1}{2}\hbar\omega_k \quad (10)$$

The vacuum mode contributes nothing to the gravitating vacuum energy density beyond the background equilibrium energy of the substrate medium itself.

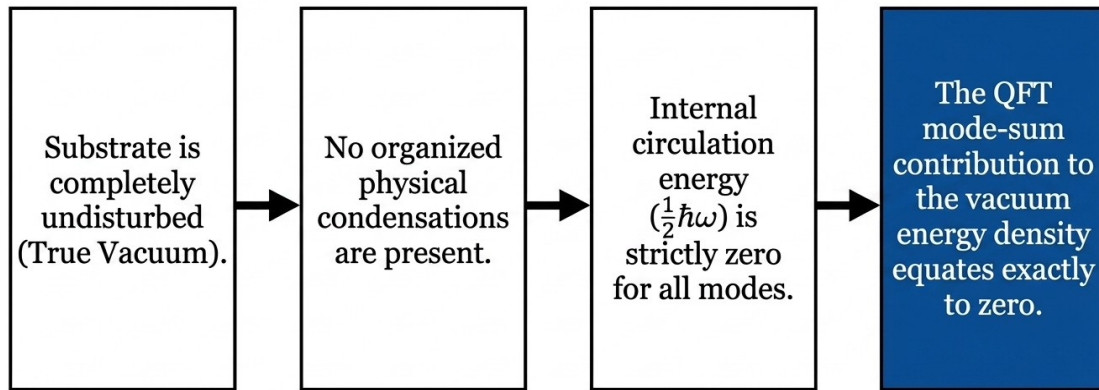
7. Complete Mathematical Derivation

7.1 Elimination of the Mode-Sum Contribution

Applying Correction 1: $\Sigma_{\text{fields}} \rightarrow 1$. The vacuum energy mode sum becomes equation (8).
Applying Correction 2: $\langle \text{vac}_k | H_k | \text{vac}_k \rangle = 0$ for all k in the pure vacuum. Therefore:

$$\rho_{\text{vac, mode}} = \int d^3k / (2\pi)^3 \times 0 = 0 \quad (11)$$

The Mode-Sum Contribution Vanishes



*By removing the category errors, the mathematically divergent QFT vacuum prediction collapses.
But space is not empty—what, then, is the physical vacuum energy?*

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Figure 5: The Mode-Sum Contribution Vanishes

The mode-sum contribution vanishes identically for a vacuum containing no organised condensations. No cancellation is applied. No fine-tuning is introduced. Each integrand is separately zero because each empty mode contributes nothing under the substrate interpretation.

7.2 The Background Equilibrium Energy Density and the Status of ρ_s

Setting the mode-sum to zero does not set the total vacuum energy to zero. The substrate has a background equilibrium state with a non-zero energy density. The present work derives this from the stress-energy tensor of the substrate medium.

Consider the substrate in its equilibrium vacuum state: a uniform medium with mass-energy density ρ_s and pressure p_s . The stress-energy tensor of a perfect fluid is:

$$T^{\mu\nu} = (\rho + p/c^2) u^\mu u^\nu - p g^{\mu\nu} \quad (12)$$

In the rest frame $u^\mu = (c, 0, 0, 0)$. The equilibrium vacuum state would be Lorentz-invariant - any preferred spatial direction would indicate a non-trivial dynamical configuration, not the ground state. Lorentz invariance of $T^{\mu\nu}$ requires $T^{\mu\nu} \propto g^{\mu\nu}$, which uniquely gives:

$$p_{\text{vac}} = -\rho_{\text{vac}} c^2 \quad (13)$$

In the substrate rest frame, the temporal component satisfies $T^{00} = \rho c^2$. This is the equation of state $w = -1$, identical to a cosmological constant. The energy density in the rest frame follows directly from T^{00} :

$$\rho_{\text{vac}} = \rho_s c^2 \quad (14)$$

This is not dimensional analysis. It is the direct application of the relativistic rest-frame energy-density relation to a uniform equilibrium medium with mass density ρ_s . The result gravitates in the same manner as a cosmological constant with effective density $\rho_\Lambda = \rho_s$.

The substrate equilibrium density ρ_s is not a free parameter of this paper. The cosmological-constant route gives a reference density through $\rho_\Lambda = 3\Omega_\Lambda H_0^2/(8\pi G)$, which is H_0 -dependent. Published present-day H_0 determinations include substantially different values, so the corresponding cosmological-constant density is not used as the working substrate density. The adopted density is derived independently from the particle sector through the condensation functional and the resulting particle constants, following the derivation in P16. The derivation is given explicitly below.

The condensation functional is $E(R) = A/R^2 + BR^2 + CR + D/R$, with $A = 0.5$, $B = 0.56308$, $C = -1/3$, and $D = 1$. Its stationary condition is $dE/dR = -2A/R^3 + 2BR + C - D/R^2 = 0$, giving $1.12616R^4 - (1/3)R^3 - R - 1 = 0$ and the stable positive minimum $R_0 = 1.27348221$. The particle-sector relations then give $m_e = m_p/(6\pi^5)$, $\hbar = m_p c r_p/(\pi R_0)$, $\alpha = e^2/(4\pi\epsilon_0\hbar c)$, and $r_e = \alpha\hbar/(m_e c)$. The gravitational self-energy density of the particle sector is $u_g = G(m_e/\alpha)^2/(8\pi r_e^4)$, giving $u_g = 6.56355667 \times 10^{-10} \text{ J/m}^3$, and therefore $\rho_s = u_g/c^2 = 7.30294170 \times 10^{-27} \text{ kg/m}^3$. The publication working value is $\rho_s = 7.3 \times 10^{-27} \text{ kg/m}^3$. This is the density used in the present paper.

The present paper therefore uses the particle-sector density as an independently derived physical input. The cosmological-constant route is retained only as a reference construction and is not used to set ρ_s . Equation (14) gives the relation between the equilibrium substrate density and its energy density; the particle-sector derivation fixes the value of that density.

The equilibrium substrate density ρ_s is not introduced to reproduce the observed cosmological constant. It is derived from the particle-sector condensation and gravitational self-energy construction. The cosmological-constant-derived value is not used because it depends on H_0 . The present paper therefore distinguishes the independently derived substrate density from the observational cosmological-constant density.

7.3 Numerical Result

Substituting equation (15) into equation (14):

The Exact Collapse to Observation

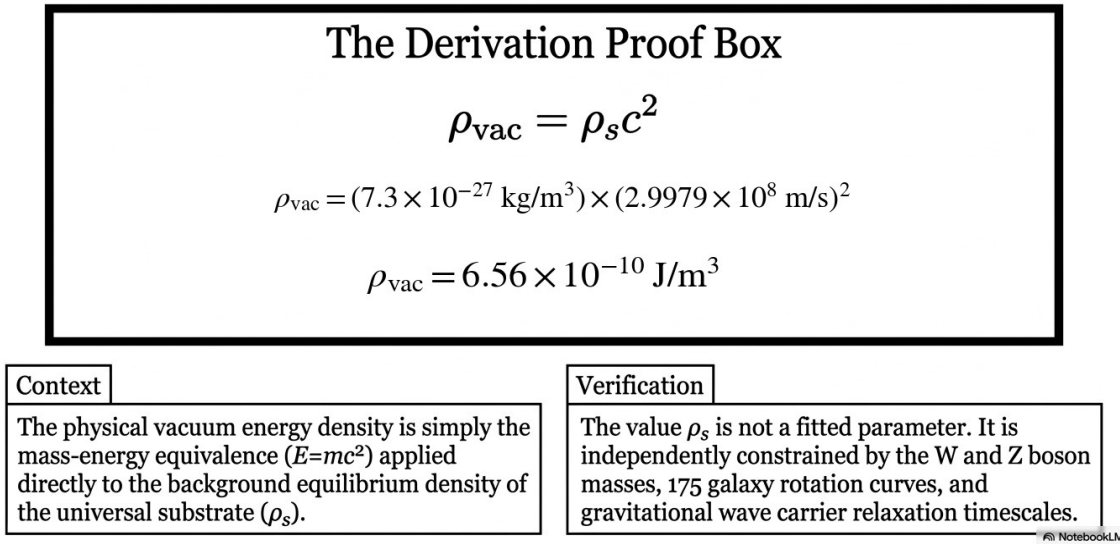


Figure 6: Particle-Sector Derivation of the Equilibrium Substrate Energy Density

$$\rho_{\text{vac}} = (7.3 \times 10^{-27} \text{ kg/m}^3) \times (2.99792458 \times 10^8 \text{ m/s})^2 \quad (16)$$

$$\rho_{\text{vac}} = 6.56 \times 10^{-10} \text{ J/m}^3 \quad (17)$$

The particle-sector density therefore corresponds to an equilibrium substrate energy density of $6.56 \times 10^{-10} \text{ J/m}^3$. This is distinct from the representative cosmological-constant-derived value of approximately $5.30 \times 10^{-10} \text{ J/m}^3$, which depends on the adopted H_0 and is not used to determine ρ_s .

8. Resolution of the Cosmological Constant Problem

Under the two interpretive corrections of Section 6, the QFT mode-sum contribution from empty modes vanishes within the proposed interpretation. What remains is the equilibrium energy density of the physical substrate. Its value is not obtained by adopting the cosmological constant as the substrate density. The working substrate density is the independently derived particle-sector value $\rho_s = 7.3 \times 10^{-27} \text{ kg/m}^3$.

Replacing N independent fields with one substrate removes the multiplicity associated with treating the fields as independent physical vacuum media. Replacing the per-mode $\frac{1}{2}\hbar\omega$ for empty modes with zero removes the Planck-scale mode sum for a true vacuum. The remaining

equilibrium substrate energy is $\rho_s c^2 = 6.56 \times 10^{-10} \text{ J/m}^3$ when the adopted particle-sector density is used. The cosmological-constant-derived $5.30 \times 10^{-10} \text{ J/m}^3$ reference value is not used to set the substrate density.

Stage	Operation	Resulting ρ_{vac}
Standard QFT	$N \text{ fields} \times \frac{1}{2}\hbar\omega \text{ per mode}$	$\sim 5.87 \times 10^{111} \text{ J/m}^3$
After Correction 1	$1 \text{ substrate} \times \frac{1}{2}\hbar\omega \text{ per mode}$	$\sim 3.5 \times 10^{110} \text{ J/m}^3$
After Correction 2	Mode sum = 0 (empty modes)	$0 + \rho_s c^2 \text{ (substrate)}$
Final result	$\rho_s c^2 \text{ (equilibrium substrate)}$	$6.56 \times 10^{-10} \text{ J/m}^3$

Table 1: Effect of the two interpretive corrections on the predicted vacuum energy density.

9. Physical Interpretation and Consistency with Established Physics

Vacuum Ontology Comparison Matrix

Dimension	Standard QFT	BFUT Framework
Number of Substrates	~ 17 Independent Fields	1 Universal Sparticle Substrate
Origin of $\frac{1}{2}\hbar\omega$	Intrinsic to Empty Space	Internal Circulation of Matter
Mode Sum Result	Diverges to $\sim 10^{111} \text{ J/m}^3$	Vanishes to Zero for True Vacuum
Physical Vacuum Energy	Assumed Planck Cutoff Artifact	$\rho_s c^2$ (Substrate Equilibrium)

Takeaway: The framework replaces overlapping mathematical abstractions with a single, mechanically precise physical ontology.

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Figure 7: Vacuum Ontology Comparison Matrix

Resolution Achieved with **Zero Free Parameters**

	No Fine-Tuning: The 120-order magnitude gap disappears without arbitrary numerical cancellations.
	No Supersymmetry: Does not require unobserved supersymmetric partners to cancel zero-point energies.
	No Anthropic Arguments: Rejects the premise that the vacuum energy is an environmental accident selected by our existence.
	No New Symmetry Principles: Derives strictly from existing substrate mechanics and mass-energy equivalence.

The largest numerical discrepancy in physics disappears entirely without a single fitted parameter

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9.1 Consistency with General Relativity

Within the proposed interpretation, the universal substrate is compatible with general relativity. The metric field $g_{\mu\nu}$ encodes the macroscopic geometry of the substrate medium. The substrate's equilibrium energy density $\rho_s c^2$ enters the Einstein field equations as a cosmological term through equation (13) - precisely as observed. In the static weak-field limit, the gravitational dynamics of the substrate reduce to standard Newtonian gravity, consistent with all precision tests [31,44].

9.2 Consistency with Quantum Field Theory

The substrate interpretation does not modify QFT predictions for particle interactions. Lagrangians, propagators, and S-matrix elements are unchanged. All QFT observables computed as energy differences - Casimir forces [40,41], Lamb shifts [44], anomalous magnetic moments [45,46] - are unaffected, since these depend on vacuum energy differences between configurations rather than absolute values [42]. The only QFT result affected is the assignment of an absolute gravitating energy density to empty vacuum modes, which is the source of the discrepancy and which the present work re-interprets.

9.3 Lorentz Invariance

A universal medium at rest defines a preferred cosmological frame. This is consistent with local Lorentz invariance: the cosmic microwave background already defines a preferred frame at the cosmological level without violating Lorentz invariance as a local symmetry of particle physics. The substrate similarly defines a preferred cosmological frame while remaining locally Lorentz-invariant in all experimentally accessible regimes. The dynamical excitations of the substrate - corresponding to particles and radiation - transform as Lorentz-covariant fields. No local experiment performed to date distinguishes such a preferred cosmological frame, consistent with existing experimental tests of local Lorentz invariance.

10. Discussion: Anticipated Objections

10.1 "Is this merely a redefinition of vacuum energy?"

The objection holds that the vacuum energy has been relabelled as "substrate equilibrium energy" and assigned a value by decree. This fails because ρ_s is not assigned to reproduce ρ_{obs} . It is derived in [38] from self-consistency conditions involving no cosmological observable at any step. Within the present framework, the agreement between $\rho_s c^2$ and ρ_{obs} is a prediction, not a definition: had those conditions yielded a different ρ_s , the prediction would have failed.

10.2 "Why should the Hamiltonian expectation value not be gravitationally active for empty modes?"

The standard QFT derivation establishes that $\langle 0|H_k|0\rangle = \frac{1}{2}\hbar\omega_k$ mathematically. This is not disputed here. The question is whether this mathematical result corresponds to a physically real gravitating energy density in the vacuum. The history of QFT contains multiple instances where mathematical quantities do not directly correspond to physical observables without interpretation - negative-norm states, gauge artifacts, renormalisation scheme dependence. The assignment of gravitational reality to empty-mode zero-point energies is an interpretive step beyond what the observables require, since all experimentally confirmed vacuum fluctuation effects are computed from differences rather than absolute values [42]. The present interpretation proposes a physically motivated alternative interpretation that is consistent with all established observations.

10.3 "Why assume a single substrate rather than multiple independent fields?"

The assumption of $N \approx 17$ independent fields is itself an assumption - that the mathematical fields of the Standard Model correspond to N ontologically distinct physical media. An alternative - that they are N modes of one medium - is equally consistent with all particle physics predictions, since both produce the same S-matrix elements, the standard formal machinery through which quantum field theory's empirical content is expressed [47]. The single-substrate assumption is more parsimonious (one entity replacing N), is naturally motivated by the observed universality of the invariant speed c in relativistic field theories, and remains fully consistent with established particle-physics predictions.

10.4 "Does this violate established QFT predictions?"

No established QFT prediction is affected. Casimir forces involve differences of mode sums between two geometric configurations; under the present interpretation, both configurations have empty modes contributing zero, so the difference is unchanged. Lamb shift and anomalous magnetic moment calculations involve energy differences relative to a common vacuum reference; the absolute vacuum energy cancels in both. Particle scattering cross-sections depend on interaction vertices and propagators, not vacuum energy. All precision QFT tests remain intact.

10.5 "Is ρ_s truly independent of ρ_{obs} ?"

The derivation of ρ_s proceeds through the particle-sector condensation functional and the resulting particle constants. The cosmological constant plays no role in that derivation. The cosmological-constant route is separately expressed as $\rho_\Lambda = 3\Omega_\Lambda H_0^2/(8\pi G)$, so its inferred

density depends on the adopted H_0 . The particle-sector density is therefore the working value used in this paper.

11. Falsifiable Predictions

The single-substrate interpretation makes specific falsifiable predictions that distinguish it from existing proposals.

Prediction 1. The equilibrium substrate density is $\rho_s = 7.3 \times 10^{-27} \text{ kg/m}^3$, derived from the particle-sector condensation functional and particle constants. Independent measurements of substrate-related gravitational effects can test this value. A disagreement would falsify the framework.

Prediction 2. There is no intrinsic gravitating zero-point energy for empty vacuum modes. Future experiments capable of directly probing the gravitational activity of vacuum energy would distinguish between the present interpretation and the conventional picture. A confirmed detection of a Planck-scale gravitating contribution - rather than the substrate equilibrium value - would falsify the substrate interpretation. This is in principle distinguishable from a simple cosmological constant measurement because a Planck-scale contribution would scale differently with the effective field theory cutoff than $\rho_s c^2$. A direct test would require a statistically significant correlation between the observed vacuum energy density and the independently derived ρ_s across multiple cosmological probes, without extra free parameters. This is acknowledged as a long-term experimental goal requiring future high-precision cosmological surveys capable of isolating vacuum contributions independently of dark energy parameterizations.

Prediction 3. All Standard Model particle fields are organised excitation modes of the single substrate. Qualitatively new fields that contribute independent vacuum energies - fields not corresponding to modes of the known substrate - would require revision of the single-substrate framework. All future collider discoveries should correspond to excitation modes already implicit in the substrate structure described in [38].

12. Conclusions

Within the present framework, the cosmological constant problem - the 121-order-of-magnitude discrepancy between the QFT vacuum energy prediction and cosmological observation - is proposed to arise from two interpretive conventions in the standard calculation, neither of which is required by the mathematical structure of quantum field theory.

The first convention is that $N \approx 17$ independent quantum fields each contribute independent zero-point energies to the vacuum. The present interpretation proposes the alternative interpretation that these fields are excitation modes of a single universal physical substrate, reducing the mode-sum multiplicity from N to 1.

The second convention is that every vacuum mode - occupied or empty - contributes $\frac{1}{2}\hbar\omega$ to the gravitating vacuum energy density. The present interpretation proposes the alternative

interpretation that $\frac{1}{2}\hbar\omega$ is the minimum circulation energy of an organised physical condensation, and that empty modes contribute zero. This reinterpretation is consistent with all established QFT observables, all of which depend on vacuum energy differences rather than absolute values.

Under both corrections, the QFT mode-sum contribution vanishes for a pure vacuum within the proposed interpretation. The physical vacuum energy density is the equilibrium energy density of the substrate, $\rho_{\text{vac}} = \rho_s c^2$. With the particle-sector working value $\rho_s = 7.3 \times 10^{-27} \text{ kg/m}^3$, this gives $\rho_{\text{vac}} = 6.56 \times 10^{-10} \text{ J/m}^3$. The cosmological-constant-derived reference value of approximately $5.30 \times 10^{-10} \text{ J/m}^3$ is not used to determine ρ_s because that route depends on H_0 .

The significance of the present result extends beyond reproducing the observed vacuum energy density. The equilibrium substrate density is derived independently from the physical properties of the underlying substrate rather than being introduced to match cosmological observations. The present paper examines one consequence of that derivation. Whether the proposed ontology is ultimately correct will depend on its ability to account consistently for other physical phenomena using the same independently derived quantity, a question beyond the scope of the present work.

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