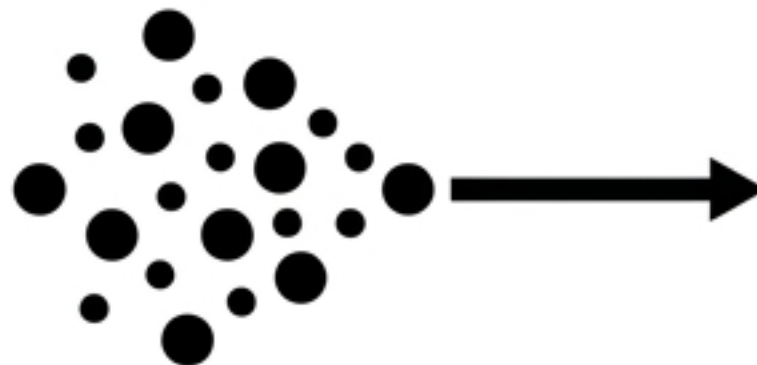


A Gravitational Sorting Resolution of the Hubble Tension

Mathematical & Statistical Formulations from BFUT Paper P60

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The Axiomatic Discrepancy: A Century of Non-Convergence

$$H_0[\text{CMB}] = 67.4 \pm 0.5 \text{ km/s/Mpc} \quad (z \sim 1100)$$

$$H_0[\text{SH0ES}] = 73.04 \pm 1.04 \text{ km/s/Mpc} \quad (z < 0.15)$$

$$H_0[\text{Group}] = 63 \pm 6 \text{ km/s/Mpc} \quad (z < 0.01)$$

$$H_0[\text{Group}] \neq H_0[\text{CMB}] \neq H_0[\text{SH0ES}]$$

Successive independent methodologies have failed to converge despite substantial improvements in measurement precision

Reframing the Velocity-Distance Relationship

Standard Cosmology

$$v = H_0 \cdot D$$

$H_0 \rightarrow$ Universal Constant

Assumes the relationship is a signature of a single, universal metric expansion rate.

P60 Gravitational Sorting

$$v \propto \underset{H_{eff}}{D} \Rightarrow \\ = f(\text{scale, binding degree})$$

$H_{eff} \rightarrow$ Emergent Statistical Property

Assumes the relationship is an emergent outcome of a gravitationally sorted population of galaxies.

The Foundational Substrate Axiom

The Spaticle Field
Equilibrium Density.

Provides the physical
framework for gravitational

$$\rho_s = 5.9 \times 10^{-27} \text{ kg/m}^3$$

Provides the physical framework
for gravitational sorting
dynamics without invoking dark
energy or metric expansion.

N-Body Simulation: Boundary Conditions

$N = 200$ galaxies (Randomized initial positions and velocities)

$a(t) = 1$ (No expansion parameter)

$\Lambda = 0$ (No dark energy term)

$\vec{v}_{init} = \text{Random}$ (No tuned initial velocity field)

Dynamics $\rightarrow$ Pure Newtonian Gravity

Can a Hubble-like velocity-distance correlation emerge purely from gravitational dynamics with no imposed metric expansion?

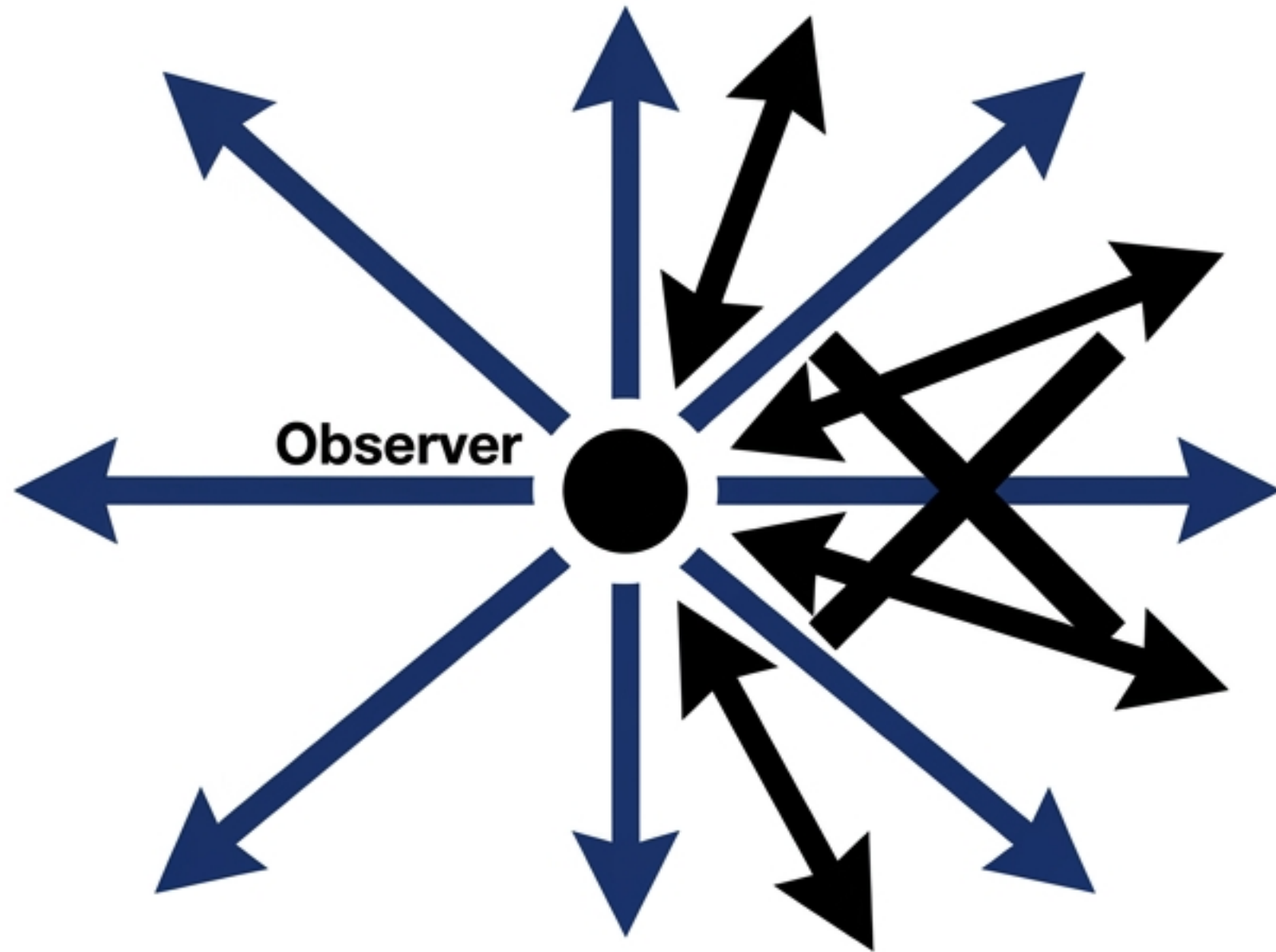
Simulation Output I: Velocity-Distance Correlation



$$\text{Eq 1: } r = 0.675$$

Pearson correlation coefficient achieved after dynamical evolution. A statistically significant velocity-distance correlation emerges purely from gravitational sorting.

Simulation Output II: The Asymmetric Survival Fraction

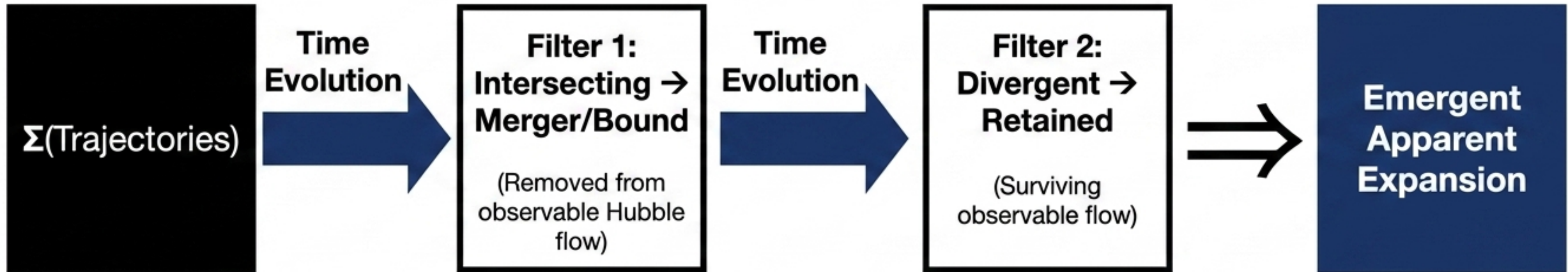


$$\text{Eq 2:}$$
$$f_{\text{recede}} = 84\%$$

Annotation

84 percent of surviving galaxies are receding from an arbitrarily chosen observer. Galaxies on interacting trajectories are preferentially removed via mergers; divergent trajectories are retained.

The Gravitational Sorting Operator



Galaxies subject to ongoing gravitational interaction develop a statistical velocity-distance relationship over long dynamical timescales.

The Scale-Dependent Sorting Formalism

$$H_{eff} \propto 1/\tau_{\text{sort}}(z, E_{\text{bind}})$$

H_{eff} : The effective velocity-distance relationship inferred by any given measurement.

τ_{sort} : Characteristic sorting timescale of the specific galaxy population.

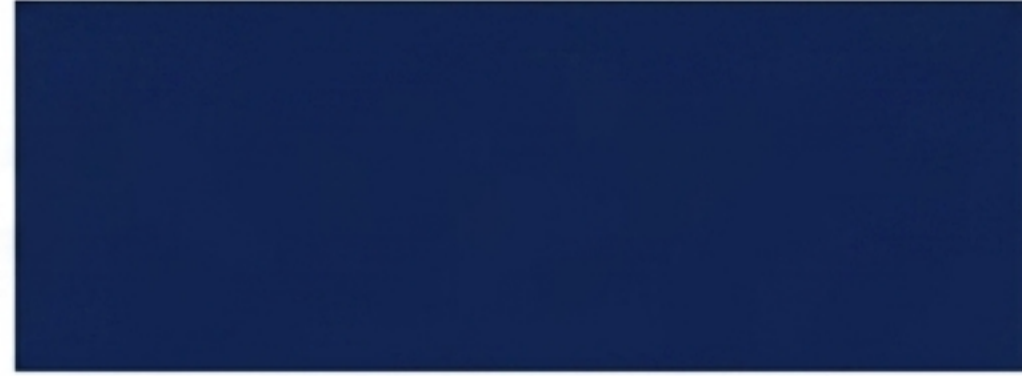
z : Redshift range.

E_{bind} : Degree of gravitational binding.

Measurements probing different spatial scales and degrees of binding are expected to return systematically different effective values of H_0 .

Mapping Observables to the Sorting Formalism

63 km/s/Mpc



High binding energy, very small scale ($z < 0.01$). Probes galaxy group infall dynamics.

67.4 km/s/Mpc



Low local binding energy, maximum scale ($z \sim 1100$). CMB-scale average where peculiar velocities average out.

73.04 km/s/Mpc



Intermediate scale ($z < 0.15$). Local distance ladder, susceptible to residual bulk-flow contamination.

Falsifiable Mathematical Predictions

$$\Delta H_0 \not\rightarrow 0 \text{ as} \\ \text{precision} \rightarrow \infty$$

Measurements will not converge to a single value as precision improves.

$$H_0(z < 0.01, \text{bound}) \\ \leq 63 \text{ km/s/Mpc}$$

Future measurements of bound galaxy groups will continue trending downward.

$$H_0[\text{SH0ES_corrected}] \\ < 73.04 \text{ km/s/Mpc}$$

Distance ladder values will drop closer to the CMB value when local bulk flow is explicitly removed.

Conclusion

The century-long pattern of non-convergence reflects a genuine physical property of the measurement. The Hubble relationship is an emergent statistical property of gravitational dynamics acting on a sorted galaxy population, rather than the signature of a single, universal metric expansion rate. ■